

Fig. 1. The electrical energy and cost required for desalinated water for RO and AD systems [22,23].

$\omega$  adsorption capacity (kg/kg)  
 $\omega_o$  maximum adsorption capacity (kg/kg)

#### Subscripts

*ads* adsorption  
*b* brine  
*ch* chilled water  
*cond* condenser  
*des* desorption  
*evap* evaporator  
*f* feed  
*hex* heat exchanger  
*hw* heating water  
*i* reverse osmosis module no in pressure vessel  
*in* inlet  
*out* outlet  
*p* permeate  
*s* salt  
*sat* saturation  
*sg* silica gel  
*sur* surrounding  
*sw* sea water  
*v* vapor  
*w* water

## 1. Introduction

Rapid growth of reverse osmosis (RO) desalination system is because it has the ability of producing desalinated water with a relatively low cost [1]. RO desalination system consists of four major components: pretreatment, high pressure pump, RO membrane modules assembly and post-treatments (permeate post-treatment and brine disposal) [2]. Intake, pretreatment and brine disposal cost of RO sea water desalination system represent about 25% of total cost [3,4].

The adsorption desalination system (ADS) is being developed steadily over the past decades and is considered one of the possible alternatives to traditional desalination systems to overcome their problems [5,6]. This technology depends on employing adsorbent materials such as silica gel. The ADS mimics the evaporation in the ambient by low temperature solar collectors and condensing water vapor at high altitude producing pure water with no need for fossil fuel. Evaporation of the seawater occurs at low-temperatures between 5 °C and 20 °C [7].

Unlike the conventional methods, adsorption technology is driven by low-grade heat such as waste heat or solar energy [6,8]. Also, ADS has few moving parts. The ADS has the ability to treat or desalinate seawater and brackish water which contain organic compounds [9]. In addition to these advantages, the ADSs produce cooling water which could reduce the dependency on the conventional electric driven cooling systems contributing to global warming with high-energy consumption.

A hybrid of Multi Effect desalination (MED) with ADS has been studied by Thu et al. [5]. AD-MED water production rate was increased to about two folds with comparing to a traditional MED while the gain output ratio (GOR) and the performance ratio (PR) had been increased by 40% [5].

Thu et al. [10] reported a hybrid AD-MED system with different numbers of effects compared to conventional MED systems. The simulation showed that the increase of AD-MED system performance is more effective at lower top brine temperature.

Shahzad et al. [11] reported that hybrid of AD-MED system could increase the desalinated water to about three folds with same top brine temperature comparing to conventional MED systems.

Thu et al. [12] proposed a hybrid AD-MED system utilizing low heat source temperature. The evaporation ensued at low temperatures ranging from 35 °C to 7 °C. This proposed cycle provided a significant high performance ratio. The specific water production, PR and GOR were about 1.0 m³/h ton of silica gel, 6.3 and 5.1, respectively. Thu et al. [13] investigated three beds two evaporators ADS. In the proposed system, COP had been increased to about 0.82 at longer cycle time.

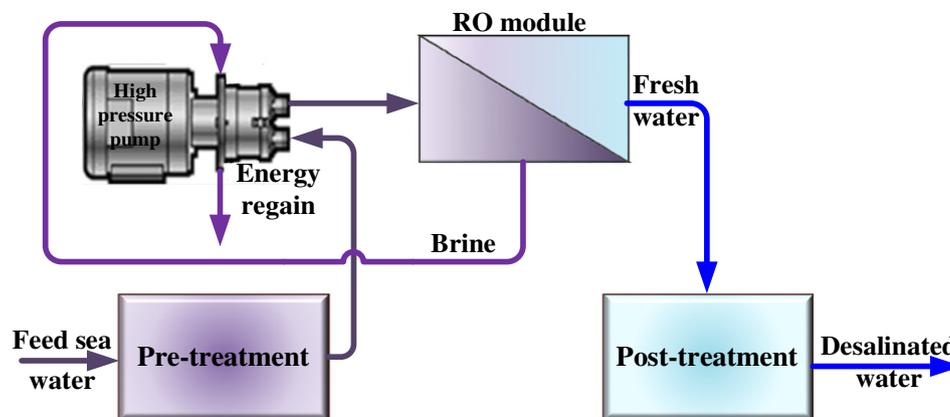


Fig. 2. RO system components.

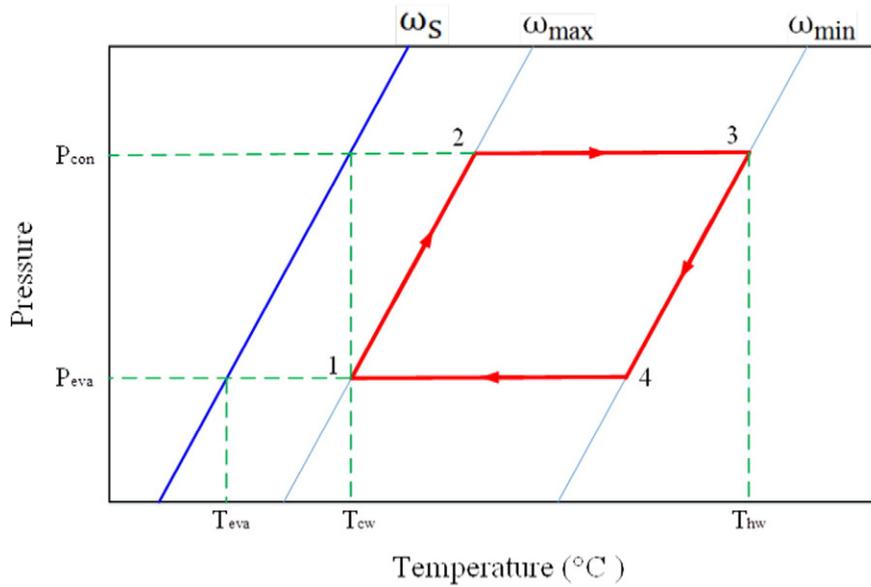


Fig. 3. P-T- $\omega$  diagram of the ideal AD cycle (1  $\rightarrow$  2 isosteric heating, 2  $\rightarrow$  3 desorption, 3  $\rightarrow$  4 isosteric cooling, 4  $\rightarrow$  1 adsorption).

Askalany [14] investigated theoretically a hybrid mechanical vapor compression with the ADS. The water production of proposed system increases by about 10–45% with comparing to ADS alone.

Performance of hybrid RO desalination system, multi-stage flash (MSF) and electro dialysis (ED) systems were also studied by Thampy et al. [15]. He presented a hybrid ED-RO system for increasing water recovery of brackish water. It was noted that the energy consumption for investigated system was from 8 to 10 kWh/m<sup>3</sup> of desalinated water with 50 to 60% recovery.

A1-Bahri et al. [16] studied the hybrid RO plant operation and MSF optimum seawater feed temperature. It had been noted that a little advantage for feed water preheating before the RO system. Marcovecchio et al. [17] investigated theoretically a model of a hybrid MSF-RO system. The investigated system was aimed to determine the optimal design operating conditions.

Helal et al. [18–20] presented a study of a hybrid MSF-RO system. This investigated study consisted of three parts: (i) modelling, problem definition and algorithm in which, the description and cost

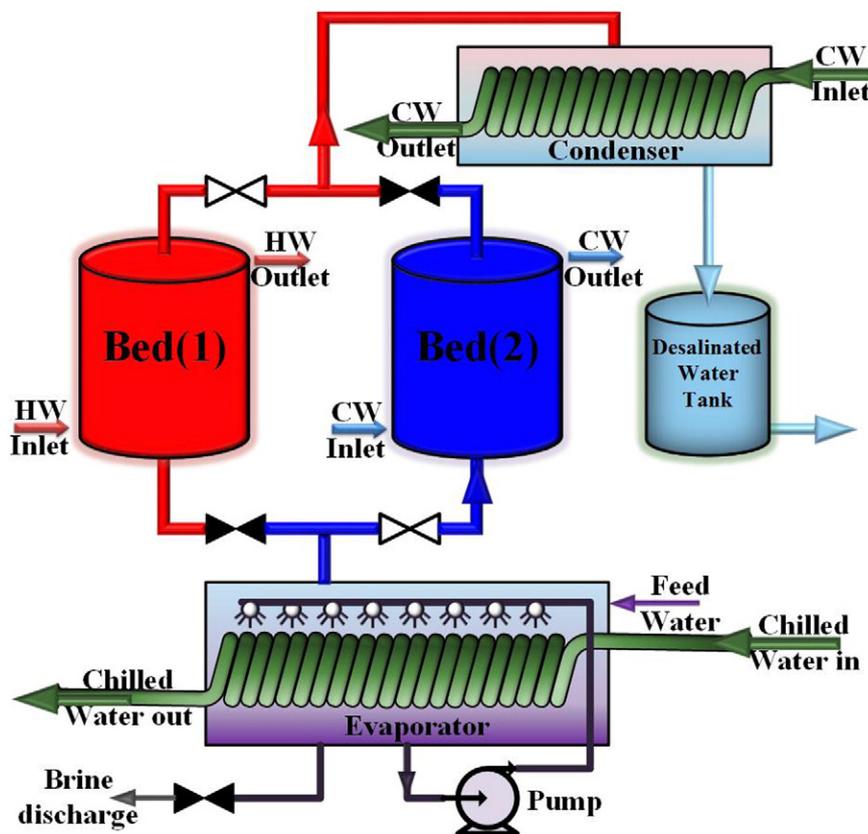


Fig. 4. ADS components [6].

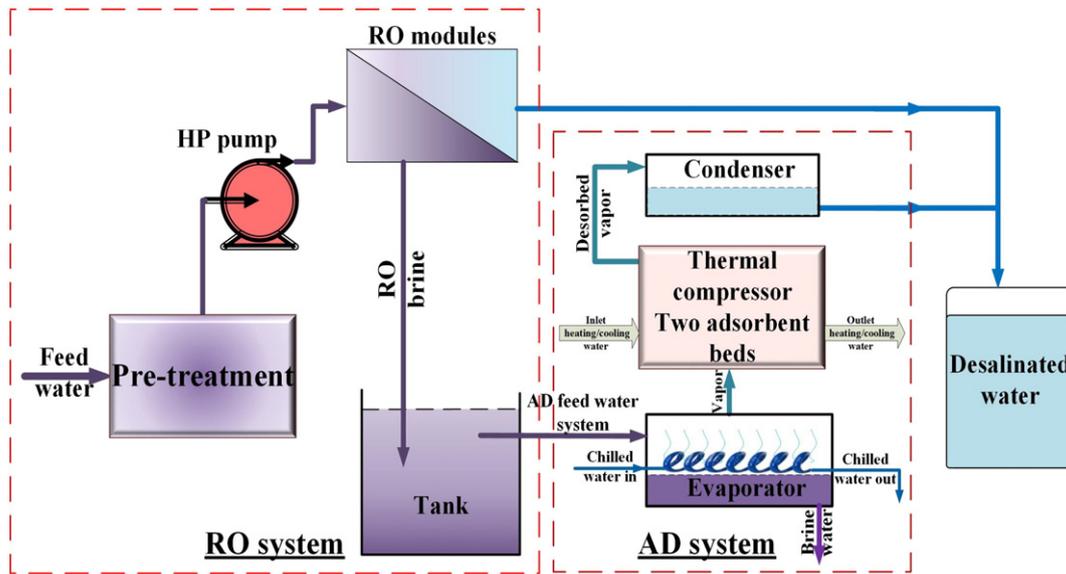


Fig. 5. Schematic of the investigated RO-AD system.

analysis were presented. (ii) Discussion and presentation of the optimal designs obtained and water costs; and (iii) discussion of sensitivity analysis.

Cardona et al. [21] presented the design of optimization tri-functional power-MSF-RO system. The optimal design of the tri-functional co-generation was based on profit maximization and exergo-economics.

Fig. 1 shows the electrical energy and cost required for production one cubic permeate of desalinated water for RO system and ADS [22–23].

This study presents RO brine recycling effect employing ADS on the required sea water feed flow rate for the same desalinated water and consequently, on the cost of desalinated water.

## 2. Physical model

### 2.1. Reverse osmosis

Main feature of the RO desalination system is its simplicity with relatively low energy consumption. RO system components are illustrated in Fig. 2 [24]. RO desalination system is an assembly of modules which are connected in a certain pattern in RO pressure vessel. For simplicity, RO pressure vessel contains four RO modules SWRHLE-440i type. The performance of RO membrane is validated with RO System Analysis (ROSA) software which its results are considered as experimental results [25,26].

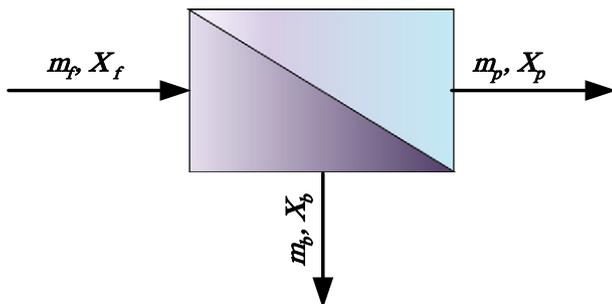


Fig. 6. One module of RO modules arrangements.

### 2.2. Adsorption desalination cycle

Adsorption desalination cycle consists of four processes as following:

- 1) Isothermic heating process: adsorbent material is heated up without changing its concentration which stays constant at the maximum concentration ( $\omega_{max}$ ).
- 2) Desorption process: adsorbent material is heated and its concentration changes from  $\omega_{max}$  to the minimum concentration ( $\omega_{min}$ ). This heat called the heat of desorption ( $Q_{des}$ ). At the same time, the released vapor is turned to liquid phase in the condenser at the condensation temperature ( $T_{cond}$ ).
- 3) Isothermic cooling process: adsorbent material is cooled down without changing the concentration which stays constant at  $\omega_{min}$ .

Table 1

The design and operating conditions [22,23,33].

Symbol	Description	Value	Unit
$A_{bed}$	Adsorbent bed heat transfer area	2.46 [32]	$m^2$
$A_{con}$	Condenser heat transfer area	3.73 [32]	$m^2$
$A_{eva}$	Evaporator heat transfer area	1.91 [32]	$m^2$
$C_{p,al}$	Aluminum specific heat	905 [32]	J/kg·k
$C_{p,cu}$	Copper specific heat	386 [32]	J/kg·k
$C_{p,ch}$	Chilled water specific heat	4200	J/kg·k
$C_{p,v}$	Water specific heat vapor phase	1890	J/kg·k
$C_{p,w}$	Water specific heat liquid phase	4180	J/kg·k
$C_{p,sg}$	Silica gel specific heat	921 [22]	J/kg·k
$D_{so}$	Diffusion coefficient	$2.54 \times 10^{-4}$ [22]	$m^2/s$
$E_a$	Activation energy	$4.2 \times 10^4$ [22]	J/kg
$H_{st}$	Heat of adsorption	$2.37 \times 10^6$ [33]	J/kg
$m \cdot w$	Cooling/heating water flow rate	1.3 [32]	kg/s
$m \cdot ch$	Chilled water flow rate	0.7 [32]	kg/s
$M_{Al}$	Bed heat exchanger fin weight (Al)	51.2 [32]	kg
$M_{con}$	Condenser heat exchanger tube weight (Cu)	27.28 [32]	kg
$M_{cu}$	Bed heat exchanger tube weight (Cu)	64.04 [32]	kg
$M_{eva}$	Evaporator heat exchanger tube weight (Cu)	12.45 [32]	kg
$M_{sg}$	Weight of silica gel in each bed	47 [32]	kg
$M_{w,eva}$	Liquid water in side evaporator initially	50 [32]	kg
$R_p$	Average radius of silica gel particle	$1.7 \times 10^{-4}$ [22]	m
$T_{ch,in}$	Chilled water inlet temperature	14	$^{\circ}C$
$T_{cw}$	Cooling source temperature	30	$^{\circ}C$
$T_{hw}$	Heating source temperature	85	$^{\circ}C$
$t_{cycle}$	Cycle time	900	s
$U_{bed}$	Heat transfer coefficient of bed	1724.14 [32]	$W/m^2 \cdot k$
$U_{con}$	Condenser heat transfer coefficient	4115.23 [32]	$W/m^2 \cdot k$
$U_{eva}$	Evaporator heat transfer coefficient	2557.54 [32]	$W/m^2 \cdot k$

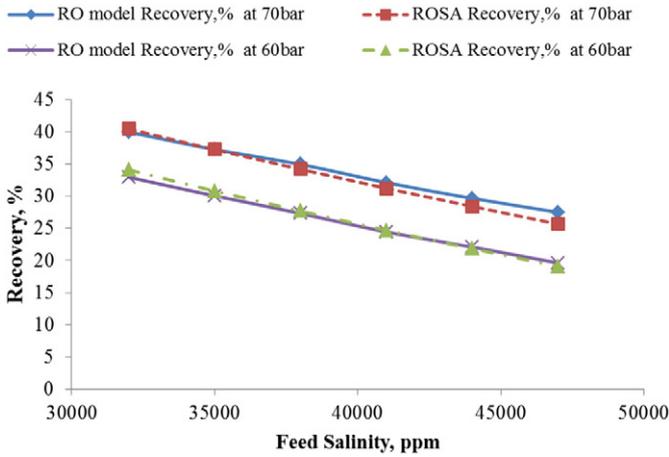


Fig. 7. RO permeate recovery with changing seawater feed salinity for the cases of 60 and 70 bar feed pressure.

4) Isobaric adsorption process: adsorbent material adsorbs vapor at  $P_{evap}$ . The concentration increases from  $\omega_{min}$  to  $\omega_{max}$  and releasing the heat of adsorption.

Fig. 3 illustrates the ideal AD cycle and Fig. 4 shows the ADS. It consists of three main parts, two adsorbent beds, condenser and evaporator as illustrated in Fig. 4. Desorption and adsorption processes are running in bed (1) and bed (2) respectively. These processes are alternatively in bed (1) and bed (2) every half cycle time [6].

The brine leaving the RO modules is fed to the ADS as shown in Fig. 5. An open air water storage tank must be added after energy recovery device of the RO system. This tank is used for solving the problem of high RO brine pressure to feed AD evaporator and the problem of intermittent duty of AD feed water intake.

The volume of the adsorbent material for ADS can be estimated by dividing brine flow in cubic meter per day of RO plant by the average of SDWP.

### 3. Mathematical model

#### 3.1. Mathematical model for RO system

The computations are based on constant feed flow rate and 25 °C temperature of seawater. Fig. 6 illustrates one module of RO system.

Osmotic pressure can be estimated by [27].

$$\pi = 0.07584 X_f \tag{1}$$

Performance of RO system is evaluated by recovery and salt rejection which are estimated as [28];

$$R = \left( \frac{m_p}{m_f} \right) \times 100 \tag{2}$$

$$SR = \left\{ 1 - \left( \frac{X_p}{X_f} \right) \right\} \times 100 \tag{3}$$

Mass and salt balances for RO system;

$$m_f = m_p + m_b \tag{4}$$

Average concentration factor is calculated by [25];

$$m_f X_f = m_p X_p + m_b X_b \tag{5}$$

$$X_{fc} = X_f \frac{\ln \left( \frac{1}{1-R_i} \right)}{R_i} \tag{6}$$

It has been noted that a slight pressure drop in feed pressure is occurred when feed water passes through the reverse osmosis element in pressure vessel. The pressure drop can be calculated by [26];

$$P_{cd} = 0.01 n q_{cave}^{1.7} \tag{7}$$

$$q_{cave} = \frac{m_f + m_b}{2} \tag{8}$$

Experimentally, the concentration polarization factor in membrane is estimated from the following [25];

$$CP = EXP(0.7 R_i) \tag{9}$$

The following equation estimates the permeate flow rate through RO membrane module [25].

$$m_p = \left( P_f - \frac{P_{cd}}{2} - P_p - \pi_{cave} + \pi_p \right) k_w A_m \tag{10}$$

$\pi_p$  and  $\pi_{cave}$  are osmotic permeate pressure and average feed side

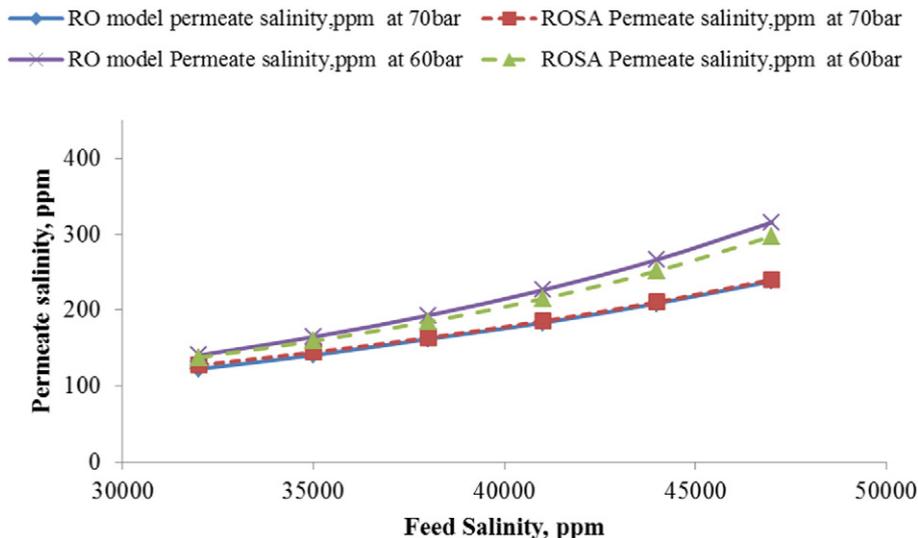


Fig. 8. RO permeate salinity with changing seawater feed salinity for the cases of 60 and 70 bar feed pressure.







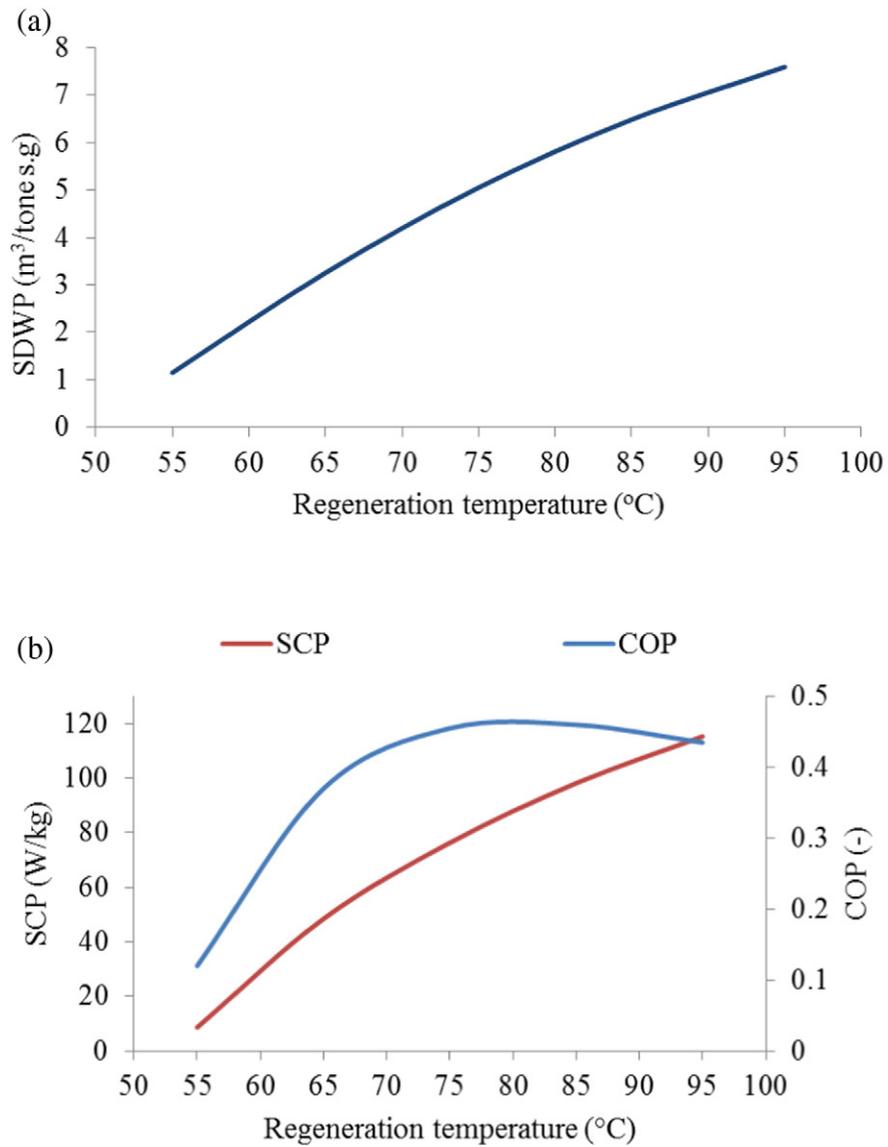


Fig. 12. AD performance parameters with changing generation temperature (a) SDWP, (b) COP and SCP.

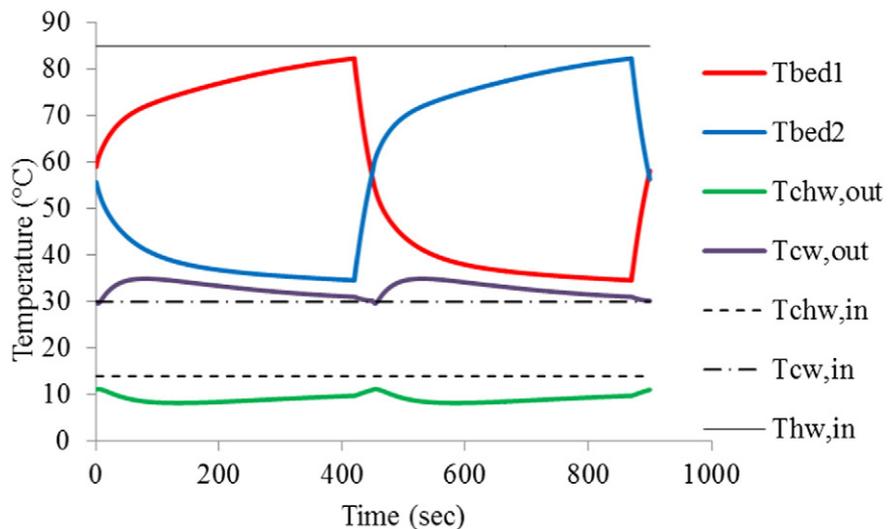


Fig. 13. AD temperature profiles for rated conditions.

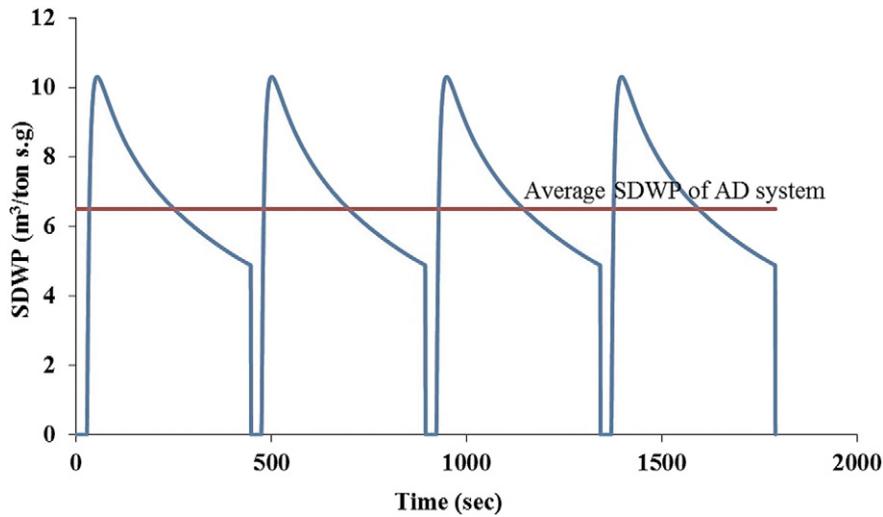


Fig. 14. The average SDWP for investigated ADS at 85 °C regeneration temperature.

coefficient of performance (COP) as following;

$$SDWP = \int_0^{t_{\text{cycle}}} \frac{Q_{\text{cond}} \tau}{h_{fg} M_{sg}} dt \quad (29)$$

$$SCP = \frac{Q_{\text{evap}}}{M_{sg}} \quad (30)$$

$$COP = \frac{Q_{\text{evap}}}{Q_{\text{des}}} \quad (31)$$

Electrical power consumptions for water pumps are neglected. The values of the designing and operating conditions are shown in Table 1 [22,32,33].

### 3.3. RO-AD system recovery

The investigated ADS has an intermittent effect of desalinated water in contrary the RO system has a continued production rate. So that water storage tank for RO brine (AD feed) has been added to solve the

problem of intermittent duty of AD intake as illustrated in Fig. 5. This open air tank must be added after energy recovery device for RO system.

Applying mass and salt balance;

$$m_{b,RO} = \bar{m}_{p,AD} + \bar{m}_{b,AD} \quad (32)$$

$$X_{b,RO} m_{b,RO} = X_{p,AD} \bar{m}_{p,AD} + X_{b,AD} \bar{m}_{b,AD} \quad (33)$$

ADS recovery is given by;

$$R_{AD} = \frac{\bar{m}_{p,AD}}{m_{b,RO}} \quad (34)$$

The overall system recovery is given by Eq. (35);

$$R_{\text{overall system}} = \frac{\bar{m}_{p,AD} + m_{p,RO}}{m_f} \quad (35)$$

EES is used for solve RO model while MATLAB is used to solve the ADS and the combination between the AD and RO.

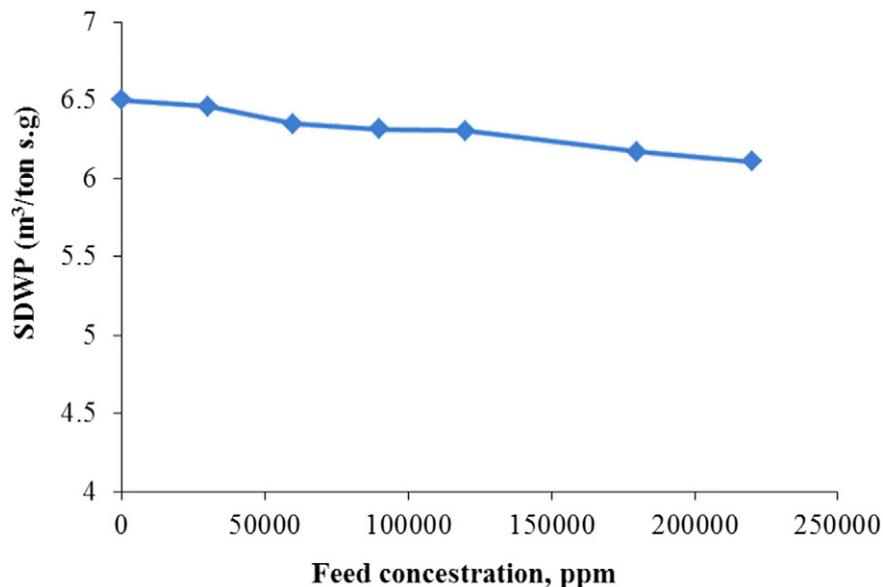


Fig. 15. The effect of feed water concentration on SDWP of ADS.



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